## TEST : MATHS $\quad$ CH9. APPLICATION OF TRIGONOMETRY CH 10. CIRCLES CH 12. AREA RELATED TO CIRCLES

## SECTION A [1 Mark each]

In fig. PA and PB are tangents to the circles with centre O. Find the value of $x$.


Q2 If the circumference is numerically equal to 3 times the area of a circle, then find the radius of the circle.

Q3 Find the perimeter of the given figure, where $\widehat{A E D}$ is a semicircle and $A B C D$ is a rectangle.
(Use $\pi=22 / 7$ )


Q4 The area of a circle is $220 \mathrm{~cm}^{2}$, find the area of the square inscribed in it.

## SECTION B [2 Mark each]

Q5 Find the length of radius of a circle whose length of tangent from an external point is 24 cm and the distance of point from where tangent is drawn from the centre is 26 cm .

In the given fig. if TP and TQ are the two tangents to a circle with centre O so
 that $\angle P O Q=140^{\circ}$, find $\angle P T Q$.

Q7 The minute hand of a clock is 10 cm long. Find the area swept by the minute hand between 9:00 am. And 9:35 am.

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\text { (Use } \pi=22 / 7 \text { ) }
$$

Q8 The perimeter of a sector of a circle of radius 5.2 cm is 16.4 cm . Find the area of the sector.

The angle of elevation of the top of a tower from a point on the ground, which is 30 m away from the foot of the tower is $30^{\circ}$. Find the height of the tower.

From the figure, prove that $\frac{\tan \theta}{\tan \phi}=\frac{1}{2}$ and it is given that 'D' be the mid - point of BC.

## SECTION C [3 Mark each]

Q11 In fig, a circle touches all the four sides of $a$ quadrilateral ABCD , whose
 sides are $A B=6 \mathrm{~cm}, \mathrm{BC}=7 \mathrm{~cm}$ and $C D=4 \mathrm{~cm}$. Find $A D$.

Q13 If all the side of a parallelogram touch a circle, show that the parallelogram is a rhombus.

Q14 A circle touches all the four sides of a quadrilateral ABCD .
Prove that: $\mathrm{AB}+\mathrm{CD}=\mathrm{BC}+\mathrm{DA}$.

ABCD is a square of side 4 cm . At each corner of the square a quarter circle of radius 1 cm and the centre of square, a circle of radius 1 cm are drawn, as shown in the figure. Find the area of the shaded region. (Use $\pi=3.14$ )
round table cover has six equal designs as shown in fig. If the radius of the cover is 28 cm , find the cost of making

the designs at the rate of Rs. 3.50 per $\mathrm{cm}^{2}$ [use $\sqrt{3}=1.7$ ]

Q17 A steel wire when bent in the form of a square encloses an area of 121 sq . cm . If the same wire is bent into the form of a circle, find the area of the circle.

Q18 A tower stands vertically on the ground. From a point on the ground 30 metres away from the foot of the tower, the angle of elevation of the top of the tower is $60^{\circ}$. Find the height of the tower.

Q19 The angle of elevation $\theta$ of a vertical tower from a point A on the ground is such that its tangent is $\frac{5}{12}$. On walking 192 m towards tower in the same straight line, the tangent of the angle of elevation $\phi$ formed to be $\frac{3}{4}$, find the height of the tower.

Q20 The angle of elevation of the top of a building from the foot of the tower is $30^{\circ}$ and the angle of elevation of the top of the tower from the foot of the building is $60^{\circ}$. If the tower is 50 m high, find the height of the building.

## SECTION D [4 Mark each]

Q21 A triangle $A B C$ is drawn to circumscribe a circle of radius 4 cm such that the segments BD and DC into which BC is divided by the
 point of contact $D$ are of length 8 cm and 6 cm respectively. Also the area of the triangle is $84 \mathrm{~cm}^{2}$. Find the sides $A B$ and $A C$.

Q22 In fig. $l$ and $m$ are two parallel tangents at A and B. The tangent at C makes an intercept DE between 1 and $m$.


Prove that $\angle D F E=90^{\circ}$.
Q23 In fig. two tangents PA and PB are drawn to a circle with centre O from an external point P . Prove that $\angle A P B=2 \angle O A B$.


Q24 ABCP is a quadrant of a circle of radius 14 cm. With AC as diameter, a semi -
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circle is drawn. Find the area of the shaded portion.

Q25 The ratio of the outer and inner perimeters of a circular path is $23: 22$. If the path is 5 m wide, then find the diameter of the inner circle.

In fig. ABC is a right angled triangle, right angled at A. Semicircles are drawn on $\mathrm{AB}, \mathrm{AC}$
 and $B C$ as diameters. Find the area of the shaded region.

In fig. the boundary of shaded region consists of four semicircular arcs, two smallest being equal. If
 diameter of the largest is 14 cm and that of the smallest is 3.5 cm , calculate the area of the shaded region.

The angle of elevation of a Jet plane from a point $P$, on the ground is $60^{\circ}$, After flight of 15 seconds, the angle of elevation changes to $30^{\circ}$. If the Jet plane in flying at a constant height of $1500 \sqrt{3} m$. Find the speed of the Jet plane.
A straight highway leads to the foot of a tower. A man standing at the top of the tower observes a car at an angle of depression of $30^{\circ}$, which is approaching the foot of the tower with a uniform speed. Six seconds later, the angle of depression of the car is found to be $60^{\circ}$. Find the time taken by the car to reach the foot of the tower from this point.

Q30 The angle of elevation of a cloud from a point 60 m above a lake is $30^{\circ}$ and the angle of depression of the reflection of the cloud in the lake is $60^{\circ}$. Find the height of the cloud.

Q31 A boy on horizontal plane finds bird flying at a distance of 100 m from him at an elevation of $30^{\circ}$. A girl standing on the roof of 20 metre high building, finds the angle of elevation of the same bird to be $45^{\circ}$. Both the boy and the girl are on opposite sides of the bird. Find the distance of bird from the girl. (use $\sqrt{2}=1.41$ )

## ANSWER

1. 4 cm
2. $\frac{2}{3}$ units
3. $(7 \pi+54) \mathrm{cm}$
4. $140 \mathrm{~cm}^{2}$
5. 10 cm
$6 . \quad 40^{\circ}$
6. $\quad 183.33 \mathrm{~cm}^{2}$
7. $15.6 \mathrm{~cm}^{2}$
8. $10 \sqrt{3} \mathrm{~m}$
9. 3 cm
10. 11 cm
11. $\quad 9.72 \mathrm{~cm}^{2}$
12. Rs 162.68
13. $\quad 154$ sq. cm
14. $\quad 51.960 \mathrm{~m}$
15. $\quad 180 \mathrm{~m}$
16. $16 \frac{2}{3} m$
17. $\mathrm{AB}=13 \mathrm{~cm}, \mathrm{AC}=15 \mathrm{~cm}$
18. $98 \mathrm{~cm}^{2}$
19. $\quad 220 \mathrm{~m}$
20. 6 sq. units
21. $\quad 86.63 \mathrm{~cm}^{2}$
22. $720 \mathrm{~km} / \mathrm{h}$
23. 3 seconds
24. $\quad 120 \mathrm{~m}$
25. 42.3 m
